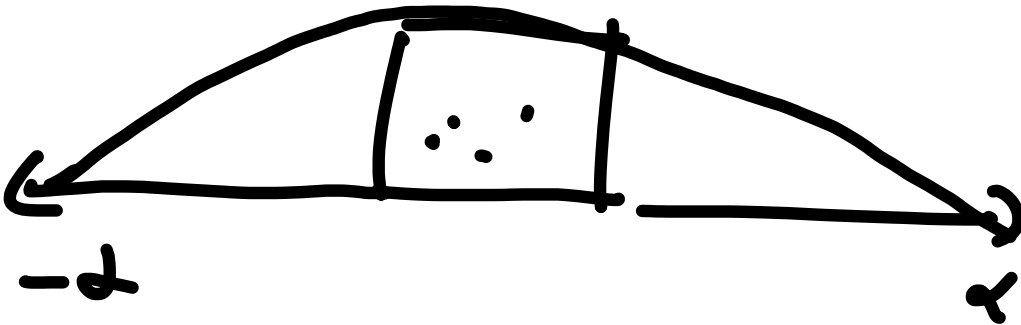


$$\int_{-\infty}^{\infty} \psi(x,t) \psi^*(x,t) dx = 1$$



$$\begin{aligned} \psi(x,t) &= A e^{-i/k(\omega t - kx)} \\ \psi(x,t) &= A e^{-i(\omega t - kx)} \\ &= A e^{-i\omega(t - x/v)} \end{aligned}$$

$$k = \frac{2\pi}{\lambda} = A^{-1} e^{i(\omega t - \frac{\omega}{v} x)}$$

$$E = h\nu = \frac{h \times 2\pi\nu}{2\pi}$$

$$= k\omega$$

$$\omega = E/k$$

$$p = \frac{h}{\lambda} = \frac{h}{2\pi} \frac{2\pi}{\lambda} = \frac{h}{\lambda} \times 2\pi\nu$$

$$\frac{p}{k} = \frac{\omega}{v}$$

$$\psi = A e^{-i/k (Et - px)}$$

$$i\hbar \frac{\partial \psi}{\partial t} = \frac{E}{k} \psi = \frac{E}{k} A e^{-i/k (Et - px)}$$

~ (1)

$$\hat{E}\psi = \hbar \frac{\partial \psi}{\partial t}$$

$$\hat{E} = \hbar \frac{\partial}{\partial t}$$

$$\hat{p}\psi = -\hbar \frac{\partial \psi}{\partial x}$$

$$\hat{p} = -\hbar \frac{\partial}{\partial x}$$

$$H = KE + PE$$

$$\hat{E}\psi = \hat{p}^2 \psi + \hat{V}\psi$$

$$\hat{E} \psi = \frac{\hat{p}^2}{2m} \psi + \hat{V} \psi$$

$$\left(\hbar \frac{\partial}{\partial t} \right) \psi = \underbrace{\left(-\hbar^2 \frac{\partial^2}{\partial x^2} \right)}_{2m} \psi + V \psi$$

$$\left. \hbar \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} + V \psi \right\}$$

SE \rightarrow .

$$\psi = A e^{-\frac{i}{\hbar}(Et - Px)}$$

$$= A e^{-\frac{i}{\hbar}Et} e^{+\frac{i}{\hbar}Px}$$

$$= e^{-\frac{i}{\hbar}Et} \left(A e^{\frac{i}{\hbar}Px} \right)$$

$$\psi = \underbrace{e^{-\frac{i}{\hbar}Et}}_{\text{time}} \underbrace{\phi(x)}_{\text{space}}$$

b)

$$i\hbar \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} + V\psi$$

$$i\hbar \frac{\partial}{\partial t} \left(e^{-i/\hbar Et} \phi(x) \right) = -\frac{\hbar^2}{2m} e^{-i/\hbar Et} \frac{\partial^2 \phi}{\partial x^2}$$

$$i\hbar \left(-\frac{i}{\hbar} E e^{-i/\hbar Et} \phi(x) \right) = -\frac{\hbar^2}{2m} e^{-i/\hbar Et} \frac{\partial^2 \phi}{\partial x^2} + V e^{-i/\hbar Et} \phi(x)$$

$$- \frac{\hbar^2}{2m} e^{-i/\hbar Et} \frac{\partial^2 \phi}{\partial x^2} + V e^{-i/\hbar Et} \phi(x)$$

2c

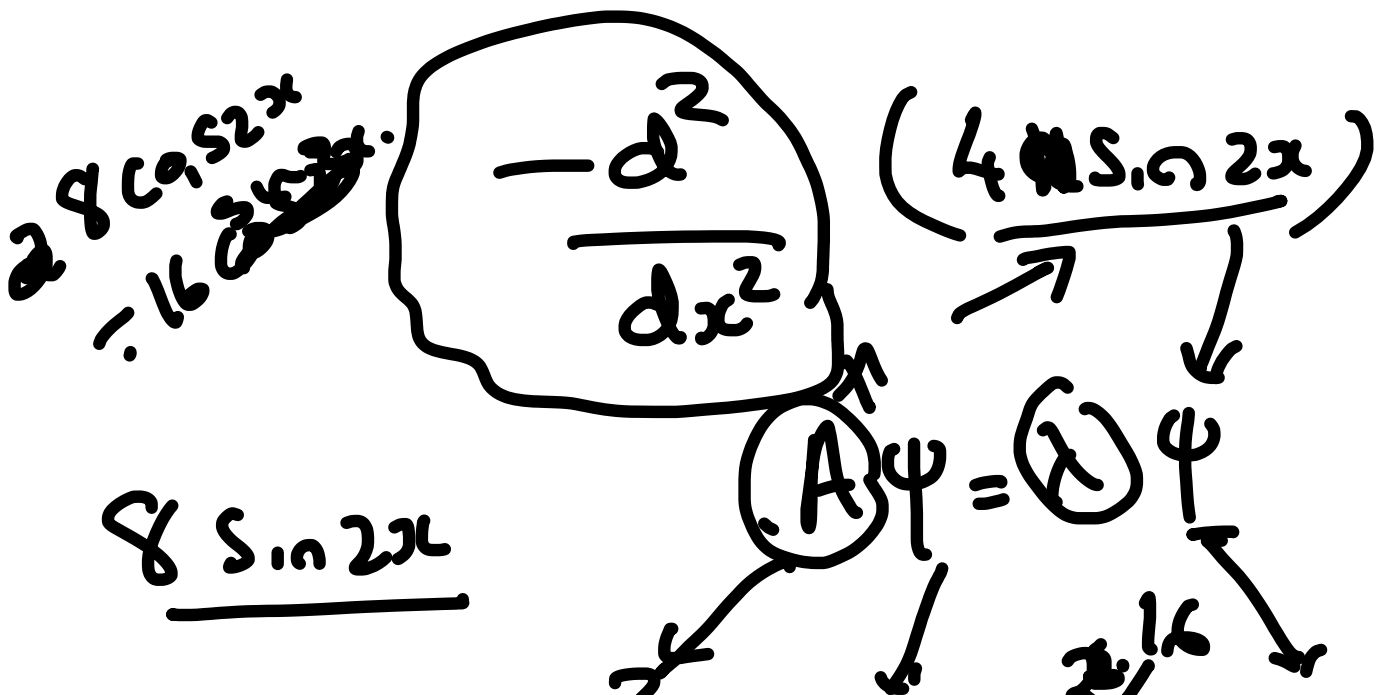
$$E \phi(x) = -\frac{\hbar^2}{2m} \frac{\partial^2 \phi}{\partial x^2} + V \phi(x)$$

Time:
$$\frac{2mE\phi(x)}{\hbar^2} = -\frac{\hbar^2}{2m} \frac{d^2\phi}{dx^2} + \frac{2mV\phi}{\hbar^2}$$

Time \rightarrow
SE

$$\frac{d^2\phi}{dx^2} + \frac{2m}{\hbar^2} (E - V)\phi(x) = 0$$

$$\nabla^2 \phi + \frac{2m}{\hbar^2} (E - V)\phi(x)$$



$$-\frac{d^2}{dx^2} (\psi \sin 2x) = \frac{2\lambda}{\psi} \sin 2x$$

$$= 4\lambda \psi \sin 2x$$

$$-\frac{d^2}{dx^2} (\psi \sin 2x) = \frac{\lambda}{\psi} \psi \sin 2x$$

λ
 ψ

$$\lambda = \frac{h^2}{p^2}$$

$$\frac{d^2 u}{dx^2} = -\frac{2m}{\hbar^2} (V - E) u$$

Chem

~~1, 2~~, 3, 4, 5, 6

Present